

# A TOPOLOGICAL APPROACH TO TENSE $n \times m$ -VALUED ŁUKASIEWICZ–MOISIL ALGEBRAS

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In 1975, Suchoń ([9]) defined matrix Łukasiewicz algebras so generalizing  $n$ -valued Łukasiewicz algebras without negation ([6]). In 2000, A. V. Figallo and C. Sanza ([4]) introduced  $n \times m$ -valued Łukasiewicz algebras with negation which are both a particular case of matrix Łukasiewicz algebras and a generalization of  $n$ -valued Łukasiewicz–Moisil algebras ([1]). It is worth noting that unlike what happens in  $n$ -valued Łukasiewicz–Moisil algebras, generally the De Morgan reducts of  $n \times m$ -valued Łukasiewicz algebras with negation are not Kleene algebras. Furthermore, in [7] an important example which legitimated the study of this new class of algebras is provided. Following the terminology established in [1], these algebras were called  $n \times m$ -valued Łukasiewicz–Moisil algebras (or  $LM_{n \times m}$ -algebras for short).

In [3], tense  $n \times m$ -valued Łukasiewicz–Moisil algebras (or tense  $LM_{n \times m}$ -algebras) were introduced by A. V. Figallo and G. Pelaitay as an generalization of tense  $n$ -valued Łukasiewicz–Moisil algebras [2]. In this paper we continue the study of tense  $LM_{n \times m}$ -algebras. More precisely, we determine a Priestley-style duality for these algebras. This duality enables us not only to describe the tense  $LM_{n \times m}$ -congruences on a tense  $LM_{n \times m}$ -algebra, but also to characterize the simple and subdirectly irreducible tense  $LM_{n \times m}$ -algebras.

## Referencias

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